

11/12/2008 A Synopsis on Science

A Synopsis on Science A Journey through 1.37 billion years of "Matter" from The Big Bang to a Green Earth

Lectures 4-6

The University of Tokyo Institute for Solid State Physics Yasuhiro Iye

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Lecture Plan

Lectures 4-6: Yasuhiro Iye "The Properties of Matter"

Lecture 4: Modern Society and Material Science
What does the discipline of Solid-State Physics do?
Lecture 5: From an Atom to a Solid Object
Diverse Matter, Varied Physicality
Lecture 6:
Manipulating Atoms, Manipulating Quanta
High-Tech and Nano-Science

Today's Talk

About Quantum Mechanics Quantum Interference, Tunnel Effect Nano-science Mesoscopic Physics Scanning Probe Microscope Macroscopic Quantum Phenomena Super-fluidity Bose Condensation Super-conduction Summary

About Quantum Mechanics

Quantum Mechanics Body of theory describing the workings of the micro world Structure of Atoms/Molecules Behavior of electrons in solids Light and Substance

Light: both a wave and a particle Electron: both a particle and wave

In saying particles and waves, it is a reflection that these are the only suitable words we have when we try and imagine quantum mechanics with everyday (classical mechanical) analogies.

> Particle nature: separate, individual Wave nature: superposition, interference

Quantum mechanical particles also display the behavior of waves

de Broglie Wavelength $\lambda = \frac{h}{\lambda}$

Momentum

de Broglie Wavelength of an electron that is accelerated at 100V

$$E = \frac{p^2}{2m} \implies p = \sqrt{2mE}$$

$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2mE}}$$

$$6.62 \times 10^{-34}$$

 $\sqrt{2 \times 0.91 \times 10^{-30} \times 100 \times 1.6 \times 10^{-19}}$ = 1.23 × 10⁻¹⁰ m λ = 0.12nm de Broglie Wavelength of a classical particle (e.g. tennis ball) is extremely short

Wave Function

The state of a particle is Described by its wave function

 $\psi(x,y,z,t)$

The existing probability of a particle is expressed by $\left|\psi(x,y,z,t)\right|^2$

The time evolution of a wave function obeys Schrödinger's equation

$$i\hbar\frac{d}{dt}\psi(x,y,z,t) = \left(-\frac{\hbar^2}{2m}\left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}\right) + V(r)\right)\psi(x,y,z,t)$$

Linear equation => Superposition Principle

$$\psi_1, \psi_2 \Rightarrow \psi_1 + \psi_2$$

=>Quantum Interference

Measurement in Quantum Mechanics

Generally, although quantum mechanics provides a probabilistic distribution of a measurable value when the measurement of a physical quality in the "same situation" is repeated, it doesn't provide a measurable value in individual cases.

By measurement, the condition becomes one of the eigenstates of that physical observable.

=> "the Collapse of wavefunction"

Time evolution is described by Schrödinger's equation and the Collapse of wavefunction occurs by measurement Standard interpretation of quantum mechanics (Copenhagen Interpretation)

Interpretation problem, observation problem of quantum mechanics Many-Worlds Interpretation

Characteristic Phenomena of Quantum Mechanics

Tunnel Effect

Passes through a potential wall it shouldn't pass through in classical dynamics

Quantum Interference Effect

 Superposition of states that pass through different paths =>Quantum Interference



Yasuhiro, IE, 2006,"Aris' Quantum Mechanics", Maruzent

Quantum Interference



The Case of Classical Particles

Yasuhiro, IE, 2006,"Aris' Quantum Mechanics", Maruzen

Probability of a bullet hitting a particular spot =Probability of it hitting the spot passing through the right slit +Probbility of it hitting the spot passing through the left slit

$$P_{\text{total}}(y) = P_{\text{R}}(y) + P_{\text{L}}(y)$$



Summation of Probability

Incident Waves



Summation of Waves' Amplitudes

Interference Pattern



The Case of Quantum Mechanical Particles

$$\Psi_{\text{total}} = \Psi_{\text{R}} + \Psi_{\text{L}}$$

Wave Function = Wave Function passing through right-hand slit + Wave Function passing through right-hand slit





Dig. 3 Representation of Electron Two-Slit Experiment

In this experiment an electron beam bi-prism is used in place of a slit. This type of experiment is technically difficult and at one time was thought of as a thought experiment that could only be done in your head. Dr Akira Tonomura (Hitachi Advanced Research Laboratory)

Double-Slit Experiment with Electrons (Dr Akira Tonomura)



Interference of Electrons



Electrons reach the screen oneby-one

An Interference Pattern will appear

Dr Akira Tonomura (Hitachi Advanced Research Laboratory)**‡** Clear proof of the wave properties of electrons





How big can something be to still Interfere?

A.Zeilinger Vienna University of Technology

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Aharonov-Bohm (AB) Effect



Mesoscopic System

Nanotechnology

Mesoscopic Physics

Micro-Scale (Microscopic)

Mesoscopic System

Macro-scale (Macroscopic)

Scale between Micro and Macro (meso: between)

The new Physics observed when the size of physical systems are comparable with or less than the scale that characterizes Physical phenomena

Miniaturisation of Semiconductor Devices



Silicon Monocrystal => Wafer => Super LSI



Cut-out Monocrystal

Wafer

Microfabrication

Moore's Law

"Integrated Circuit Complexity"



The degree of integration of LSI (Large Scale Integration), in other words, the number of transistors that can fit within a unit area will double approx. every one-and-a-half years.

Nano-science / Nanotechnology

- Semiconductor technology⇒ More than Moore Can't simply miniaturise
 - Problem of heat production
 - Problem of quantum fluctuation
- Nano-science
 - Observing atoms, Manipulating atoms
 - There are new quantum physics effect in the Nano world "There is plenty of room at the bottom." (Richard Feynman)

Mesoscopic Physics

Aharonov-Bohm (AB) Effect





Quantum Resistance

Make quanta that have the dimensionality of electrical resistance from physical constants



$$\frac{h}{e^2} = 25.813 \,\mathrm{k}\Omega$$

$$\frac{e^2}{h} = \frac{1}{25,813 \,\mathrm{k}\Omega} = 38.7 \,\mu\mathrm{S}$$

Quantum Resistance Quantum Conductance

Quantum Conductance

 $\frac{e^2}{h} = \frac{1}{25.813 \,\mathrm{k}\Omega}$

Quantum Hall Effect => International Standard of Resistance

Superconductor-Insulator Transition



Mono-Electron Tunnel Effect

Nano-Tunnel Junction



Coulomb Island (Quantum Dot)

The electrostatic potential of the island increases as one electron tunnels => next electron can't enter

Coulomb Blockade

 $l \mu m$

Quantum Dot (Artificial Atom)



Periodic Law of Artificial Atoms





source: Shingo, Tarucha, Graduate school of Science



Observing Atoms Manipulating Atoms

The Small Scale



Observing Small Things : Electron Microscope





0000 0000

500

10

Observe the arrangement of atoms with a High-Resolution Electron Microscope



a-SiC H.Ichinose The University of Tokyo

Observing the arrangement of atoms of a solid surface



Is this type of thing possible on the atomic scale? => common sense tells us that it's "impossible"

Scanning Tunnel Microscope 1984 Binnig and Rohrer

First picture taken of the arrangement of atoms on the surface of a silicon crystal

Scanning Tunnel Microscope (STM)



When the atoms of the needle tip and atoms of the surface get to within 1nM of each other, the Tunnel Current flows Similar to the tunnel current becoming constant, if the pin moves laterally as it rises and falls you can observe the irregularity of the atom scale

Atomic Force Microscope (AFM)



A probe on the end of a cantilever (one-ended beam)

Detect the force when the atoms on the end of the probe get close to the atoms of the surface



Detect the force when the atoms on the end of the probe get close to the atoms of the surface



Manipulating Atoms



image © Crommie, Lutz & EiglerIBM

image © Lutz & Eigler IBM

Arranging Iron atoms on a Copper surface. The ripple-like appearance is due to the wave interference of the surface electrons Macroscopic Quantum Phenomena Bose Condensation and Super-conduction

Quantum Mechanical Particles

Cannot discriminate between quantum mechanical particles of the same type

Even when two particles interchange, the state remains the same as before (However, the wave function will generally have a numerical factor)

 $\Psi(b,a) = C\Psi(a,b)$ $\Psi(a,b) = C\Psi(b,a) = C^2\Psi(a,b)$ $\Rightarrow C^2 = 1$ $\Rightarrow C = 1 \text{ or } -1$

Bose Particle

Fermi Particle

Quantum Statistics

Bose Particle (Boson) Spin: 0,1,...



Fermi Particle (Fermion)

Spin: 1/2, 3/2, ...



 $\Psi(b,a) = -\Psi(a,b)$

If a=b then $\Psi(a,a) = -\Psi(a,a)$ $\Psi(a,a) = 0$



Any number can enter the same state

Only one can enter the same state (Pauli Exclusion Principle)



Maxwell Boltzmann Distribution at the High Temperature Limit

$$f(E) = e^{-(E-\mu)/k_{\rm B}T}$$

Helium Isotopes



³He 2 Protons 1 Neutrons 2 Electrons Total Spin = 1/2 Fermi Particle

Making Ultra-Low Temperatures

Ultra-low temperatures are required to observe phenomena that behave in a quantum statistical manner



Inner structure of a Liquid Helium Container

Liquid Nitrogen 77K Liquid Helium (⁴He) 4.2K Decompression with a vacuum pump ~1.2K Liquid Helium (³He) 3.2K Decompression with a vacuum pump ~0.3K ³He-⁴He Dilution Refrigerator ~ mK Adiabatic Nuclear Demagnetization ~ μ K

Phase Diagram of Helium



Helium atoms:
1)Light
2)Weak Interaction
Kinetic Energy >
Interaction Energy

Helium (at normal pressure) will not become a solid even at absolute zero => Quantum Liquid





Super-fluidity of Liquid Helium



The University of Tokyo Cryogenic Research Center



Quantum Vortex

Macroscopic Wave Function
$$\Psi = \Psi_0 e^{i\theta}$$

Quantization of Circulation

$$\kappa \equiv \oint_C \mathbf{v}_s \cdot d\mathbf{s} = \frac{\hbar}{m} \oint_C \nabla \theta \cdot d\mathbf{s} = \frac{\hbar}{m} 2\pi n = n \frac{h}{m}$$

Permanent Current

Quantum Vortex











Bose-Einstein Condensation



Bose Condensation when the Thermal Thermal de Broglie Wavelength X

$$\lambda_{\rm T} = \left(\frac{2\pi\hbar^2}{mk_BT}\right)^{1/2}$$

$$\lambda_T \approx n^{-\frac{1}{3}}$$

$$T_{\rm BE} = \frac{2\pi\hbar^2}{mk_{\rm B}} \left(\frac{n}{2.612}\right)^{\frac{2}{3}}$$

Laser Cooling of Atomic Gases Collect and cool an atomic (e.g.Rb) gas (vapor) in a trap Doppler Cooling

 Shine light at a frequency just below the resonance frequency of the atoms

•To the atoms travelling in the opposite direction to the light, the frequency of this light looks higher and becomes closer to the resonant frequency due to the Doppler effect, so the absorption probability becomes higher. The atoms decelerate due to the light absorbing the momentum.

•When the light is re-shone, it is shone isotropically so on average the atoms decelerate.

• Due to six laser beams being shone in x, y, z axes, Doppler cooling occurs in every direction

•The limit of Doppler Cooling is about $T \sim 100 \,\mu$ K =>this temperature can lower a further 3-4 orders of magnitude

hν

Bose-Einstein Condensation of Atomic Gases

Reducing the temperature and achieving the conditions of Bose-Einstein Condensation by Evaporative Cooling of atomic gas cooled in a magnetooptical trap $T \sim 10^{-7}$ K $\lambda_T \approx n^{-1/3}$ On shutting off the trap, the velocity distribution consequently swells as the atomic gas falls under the force of gravity.



Super-fluidity of ³He

Phase diagram of ³He



³He becomes a superfluid at the ultra-low temperature of ~2mK Although the ³He Fermi particle doesn't undergo Bose Condensation, transition into Superfluid state can occur when 2 ³He molecules pair and behave like a Bose particle (Same mechanism as Super-Conduction)

Basic Properties of Super-Conduction



Magnetic Field if repelled in the Super-Conducting State

Observation of Magnetic Flux Particles





Bitter Method (Essmann & Traueble, 1968)

Lorentz Microscope (Tonomura Akira, 1992) Scanning Tunnel Microscope (Hess, 1989) t

Mechanisms of Super-conduction

Cooper Pair Configuration

Origin of Attraction? Electron Particle Interaction

(+)

(+)

+





When the inter-electron attractive force mediated by electron lattice interaction over-powers the inter-electron Coulomb repulsive force, pure attraction is able to function.

When attractive force acts on 2 electrons on the Fermi plane, a bound state (Cooper Pair) takes shape.

Super-conduction Transition Temp.

7

+

+

(+)

$$T_{\rm c} = 1.14\Theta_{\rm D} \exp\left(-\frac{1}{N(0)V}\right)$$



Future Predictions of Technological Development

VS

Predictions of the Development of Science

"Integrated Circuit Complexity"



Gordon E.Moore "NO EXPONENTIAL IS FOREVER..."

Load Map ⇒ Self-fulfillment Prophecy



Summary

Characteristic of Quantum Mechanics Quantum Interference, Tunnel Phenomenon Mesoscopic Physics Quantum Conductance e²/h Quantum Interference AB Effect Mono-electron Tunnel Effect Nanotechnology Nano-science Observing Atoms, Manipulating Atoms Scanning Probe Microscope Macroscopic Quantum Phenomena Super-Fluidity Bose Condensation Super-Conduction

Positioning of Solid-State Physics

- Understanding the various provided softwarious substances (Solid-State Powercies) based on the basic principles of photol (Quantum Physics)
 And hase Transition and component which has a unit metally and unity within variation and component of the software of Quantum Mechanics
 Becoming a software of Quantum Mechanics
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